

# Implementing a Layered Models based Query-Solving Engine

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# Outline

- 1 Motivation
- 2 Layering Logic Programs
  - Background
  - Layering
  - Properties
- 3 Implementation
- 4 Conclusions

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# Motivation

- NLPs are commonly used for KRR
- The current standard 2-v semantics (Stable Models) does not deal appropriately with all NLPs

## Example

```
    beach ← not mountain
    mountain ← not travel
    travel ← not beach, passport_ok
    passport_ok ← not expired_passport
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- What is the semantics of this program? SMs say the only solution is  $\{expired\_passport, mountain\}$
- What if the passport is ok? SMs say:  
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## Background Notions (i)

### Definition

A Logic Rule  $r$  has the general form

$$A \leftarrow B_1, \dots, B_n, \text{not } C_1, \dots, \text{not } C_m$$

where  $A$ , the  $B_i$  and the  $C_j$  are atoms.

We say  $A$  Directly Depends on each  $B_i$  and on each  $C_j$ .

Dependency being the transitive closure of Direct Dependency.

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A non ground rule stands for the whole collection of its ground instances

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## Background Notions (ii)

### Definition

Two atoms ***a*** and ***b*** are in a loop iff they depend on each other.

*passport\_ok* ← *not expired\_passport*  
*expired\_passport* ← *not passport\_ok*

*passport\_ok* and *expired\_passport* are in an Even Loop Over default Negation (ELON).

*beach* ← *not mountain*  
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*beach*, *mountain*, and *travel* are in one same OLON.

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- Usual notion of stratification says: atom  $a$  is in a stratum above of  $b$  iff  $a$  depends on  $b$
- Consequence: both even and odd loops are *unstratifiable*
- Usual notion of support says: an atom  $a$  is supported in a model  $M$  iff **all** the literals of at least one body of a rule for  $a$  are true in  $M$

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## Layering — Intuitive Idea (i)

- Layering is a generalization of stratification that tackles all kinds of loops
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  - two atoms  $a$  and  $b$  are in the same layer iff they are in a loop with each other
  - if atom  $a$  depends on  $b$  and they are not in a loop with each other, then  $a$  is *strictly above*  $b$
- Consequence: all NLPs are *layerable* (a loop's rules are in the same layer)
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*passport\_ok* ← *not expired\_passport*      Layer 1  
*expired\_passport* ← *not passport\_ok*

# Layering — Intuitive Idea (ii)

## Example

*beach* ← *not mountain*  
*mountain* ← *not travel*                      Layer 2  
*travel* ← *not beach, passport\_ok*

*passport\_ok* ← *not expired\_passport*              Layer 1  
*expired\_passport* ← *not passport\_ok*

# How to Compute Layered Models — Iterative Method

- 1 Compute the Layers  $L_1, \dots, L_n$  of  $P$
- 2 Compute a Minimal Model  $M_1$  of layer  $L_1$
- 3 For each layer  $L_{i+1}$ 
  - ⊖ Reduce  $L_{i+1}$  by  $M_i$ , i.e. remove body literals true in  $M_i$
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# Layered Models of the Example

## Example

$b \leftarrow \text{not } m$   
 $m \leftarrow \text{not } t$   
 $t \leftarrow \text{not } b, p\_ok$

$p\_ok \leftarrow \text{not } exp\_p$   
 $exp\_p \leftarrow \text{not } p\_ok$

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$t \leftarrow \text{not } b$

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## Example

$$\begin{array}{l}
 b \leftarrow \text{not } m \quad M_{2,1} = \{b, m, p\_ok\} \\
 m \leftarrow \text{not } t \\
 t \leftarrow \text{not } b
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$t \leftarrow \text{not } b \quad M_{2_3} = \{b, t, p\_ok\}$

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 $exp\_p \leftarrow \text{not } p\_ok$        $M_{1_2} = \{exp\_p\}$

# Layered Models of the Example

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$m \leftarrow$

$p\_ok \leftarrow not\ exp\_p$

$exp\_p \leftarrow not\ p\_ok$

$M_{1_2} = \{exp\_p\}$

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$m \leftarrow M_{2_4} = \{m, \text{exp\_p}\}$

$p\_ok \leftarrow \text{not exp\_p}$   
 $\text{exp\_p} \leftarrow \text{not } p\_ok \quad M_{1_2} = \{\text{exp\_p}\}$

## Details about Properties

- **Relevance:** a semantics is relevant iff

$$\forall_a a \in \mathit{Sem}(P) \Leftrightarrow a \in \mathit{Sem}(\mathit{Rel}_P(a))$$

Only relevant semantics can benefit from top-down query-solving

- **Cumulativity:** a semantics is cumulative iff

$$\forall_{a,b} (a \in \mathit{Sem}(P) \wedge b \in \mathit{Sem}(P)) \Rightarrow a \in \mathit{Sem}(P \cup \{b\})$$

Only cumulative semantics can benefit from tabling methods

# Properties of Layered Models Semantics

Property	SMs	LMs
Existence Relevance Cumulativity Classical Support Layered Support		

# Properties of Layered Models Semantics

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# Properties of Layered Models Semantics

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Moreover,

- $LMs \supseteq SMs$  for any NLP

# Properties of Layered Models Semantics

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Existence	No	Yes
Relevance	No	Yes
Cumulativity	No	Yes
Classical Support	Yes	No
Layered Support	No	Yes

Moreover,

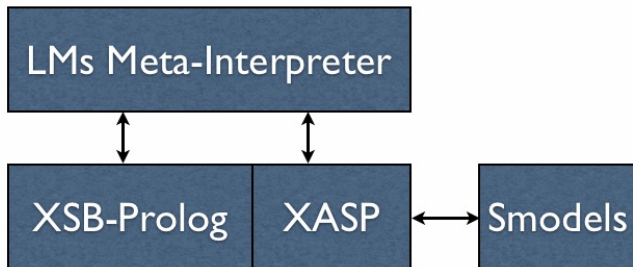
- $LMs \supseteq SMs$  for any NLP
- When the NLP has no OLONs,  $LMs = SMs$

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## Implementation Architecture

Implementation is via a meta-interpreter written in XSB-Prolog.  
Takes advantage of XSB's XASP interface to Smodels.



# Implementation's Query Solving Steps — `lmquery/2` predicate

- Load the KB in the input NLP
- Accept a query from the user
- Identify the part of the NLP relevant for the query (residuum)
- In a “top-down” (Prolog-like) fashion, traverse each call-graph branch in the residuum, and identify and solve the OLON (if there is any) along the branch  
Identifying and solving OLONs naturally respects the layering
- Send the relevant part of the NLP, along with the solved OLONs, to Smodels via XASP
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- Load the KB in the input NLP
- Accept a query from the user
- Identify the part of the NLP relevant for the query (residuum)
- In a “top-down” (Prolog-like) fashion, traverse each call-graph branch in the residuum, and identify and solve the OLON (if there is any) along the branch  
Identifying and solving OLONs naturally respects the layering
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## OLON resolution in the Example

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OLON is detected! Depends on *passport\_ok*

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On backtracking each alternative rule is sent along with the  
rest of the residuum to Smodels.

# Outline

- 1 Motivation
- 2 Layering Logic Programs
  - Background
  - Layering
  - Properties
- 3 Implementation
- 4 Conclusions

# Conclusions

- Stable Models are a very important step, but we can take another step forward
- Introduced new (layered) notion of support (extends the usual notion)
- New 2-valued semantics for NLPs
  - is conservative extension to SMs
  - guarantees model existence, enjoys relevance and cumulativity
- Implemented Query-Solving Engine

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## Future Work

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- Implement a full-fledged query answering Layered Models engine for first order NLPs at WAM level (already underway in cooperation with XSB)
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## References

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# Demo

Let's see a demo  
of the example!

# Thank you!

## FAQs

- Layering calculation complexity? Computing Layering = Finding SCCs = Quadratic
- Layer  $L_{i+1}$  reduction by  $M_i$ :
  - remove all rules from  $L_{i+1}$  with *not*  $a$  in the body where  $a \in M_i$
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- Integrity Constraints (ICs) are now written as
$$\text{falsum} \leftarrow \text{Body\_of\_IC}$$
instead of
$$\text{falsum} \leftarrow \text{not falsum}, \text{Body\_of\_IC}$$
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